

**AMS-205B WINTER 2016  
HOMEWORK 1**

All numbers refer to Casella & Berger, Statistical Inference, Second Edition, Duxbury.

- (1) Problem 5.2.
- (2) Problem 5.3.
- (3) Problem 5.8.
- (4) Problem 5.10.
- (5) Problem 5.16.
- (6) Problem 5.17.
- (7) Problem 5.21.
- (8) Problem 5.24.
- (9) Problem 5.27.
- (10) Problem 5.36.
- (11) Problem 5.42.
- (12) Let  $X_1, \dots, X_n$  be an iid sample with  $X_i \sim N(\mu, \theta^2)$ . Use the definition of convergence in probability and the fact that  $\sum_{i=1}^n (X_i - \mu)^2 / \sigma^2 \sim \chi_n^2$  to show that  $\sum_{i=1}^n (X_i - \mu)^2 / n$  converges in probability to the constant random variable  $\sigma^2$  as  $n \rightarrow \infty$ .